

# Visualization of Structure-Property Relationships: Spanning the Length Scales (nano to macro)

[http://www.jwave.vt.edu/~rkriz/Pubs/NSF\\_SEVC/NSF\\_sevc.doc](http://www.jwave.vt.edu/~rkriz/Pubs/NSF_SEVC/NSF_sevc.doc)

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by

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## Description (100 words)

Recent development of networked collaborative immersive software [1-3] allows more accurate visual analysis of complex connected wave-velocity surfaces propagating through anisotropic crystals. Existing topologies, used for sub-classification within orthorhombic symmetry [4-6], were studied using these immersive tools. From Christoffel's equation the fourth order elastic stiffness tensor,  $C_{ijkl}$ , uniquely defines these topologies where the collection of all wave speeds,  $v$ , (topology) and their vibration directions,  $\hat{\mathbf{n}}_k$ , correspond to the wave propagation direction,  $\hat{\mathbf{k}}$ , and color is defined by  $\hat{\mathbf{n}}_k \hat{\mathbf{n}}_k$  [7]. Together both topology and color uniquely represent  $C_{ijkl}$  for  $\text{Ca}[\text{HCOO}]_2$ . Insight occurs when the observer is "immersed" inside the crystal (nano-structure) and the wave velocity (macro-property) topology. Polar covalent bond orientations are seen to align along stiffer directions where faster longitudinal wave speeds appear as purple bulges.

## REFERENCES

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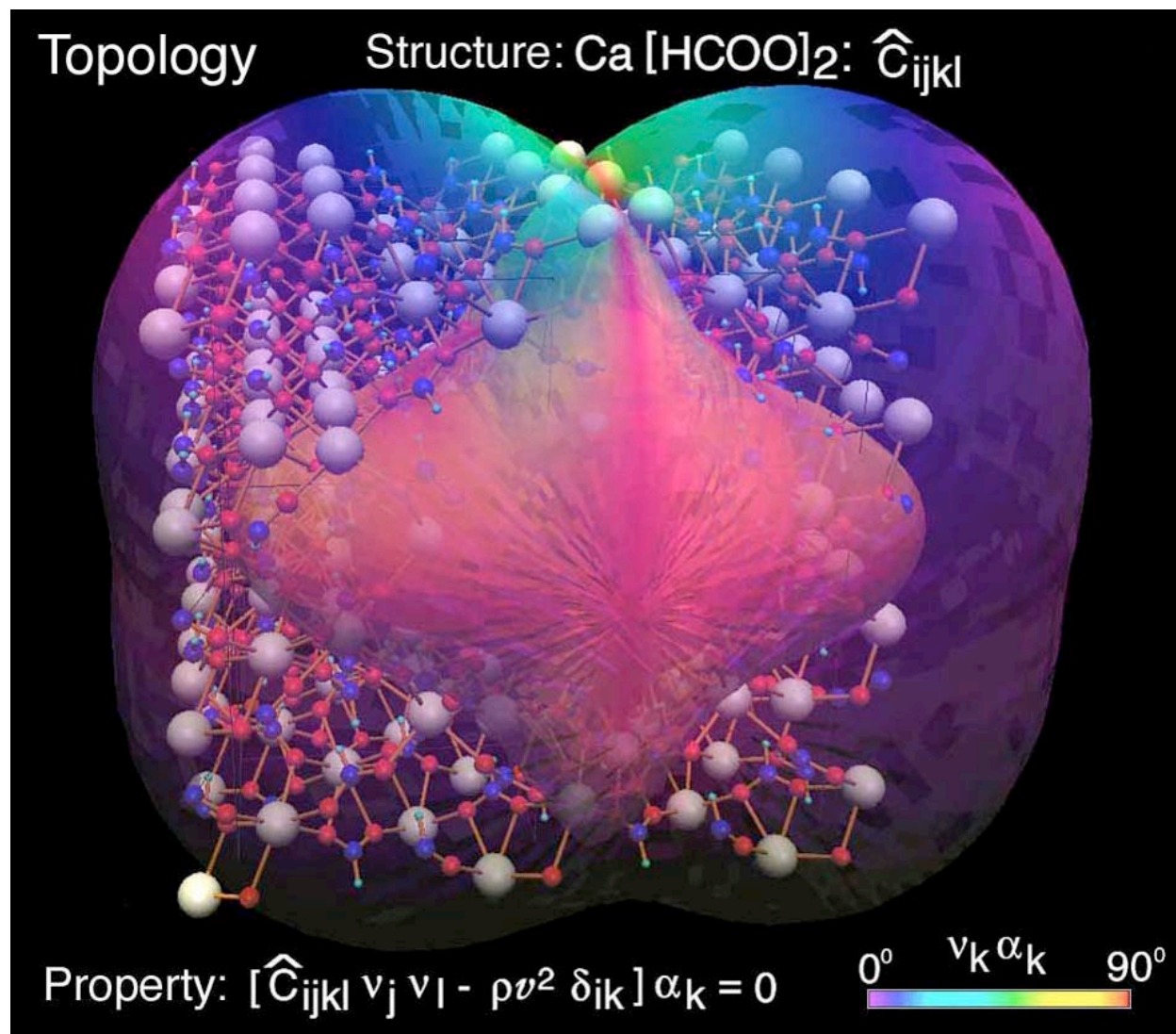
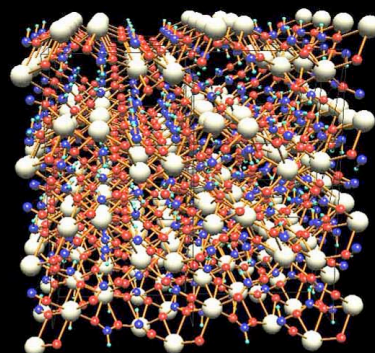
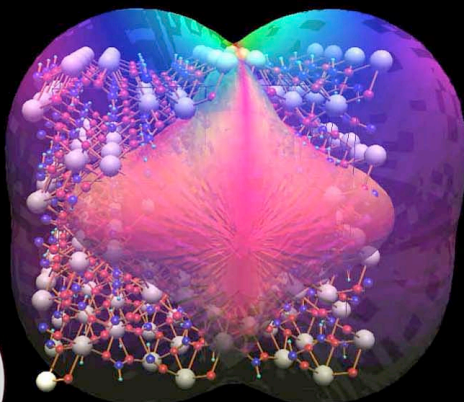
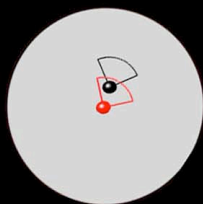


Figure 1a. Nano-Macro Topology for  $\text{Ca}[\text{HCOO}]_2$

# Visualization of Structure Property Relationships

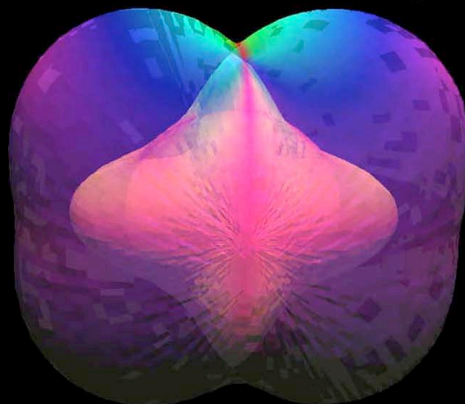
Spanning the Length Scales (nano to macro)

Remote site  
"avatar"  
participating in  
a networked  
immersive  
virtual  
environment



Structure (nano):  $\text{Ca} [\text{HCOO}]_2, \hat{C}_{ijkl}$

Property (macro):  $\nu(\hat{C}_{ijkl})$  and  $\nu_k \alpha_k(\hat{C}_{ijkl})$



$\hat{C}_{ijkl}$  property visualized as

Wave Topology: Shape ( $\nu$ ) and Color ( $\nu_k \alpha_k$ )

Christoffel's equation:  $[\hat{C}_{ijkl} \nu_j \nu_l - \rho \nu^2 \delta_{ik}] \alpha_k = 0$

Wave Type : Longitudinal  $\nu_k \alpha_k$  Transverse

0° 90°

Figure 1b. Description of Nano-Macro Topology for  $\text{Ca}[\text{HCOO}]_2$