

ESM 2204 - FINAL EXAMINATION
MECHANICS OF DEFORMABLE BODIES
EXAMPLE

NAME _____
(print) _____
last _____ first _____ initial _____

PLEDGE (signature): On my honor I have neither given nor received unauthorized aid on this test.

INSTRUCTIONS:

Closed book, closed notes.

There are 13 questions on this exam - check for completeness. Part I (40%) consists of 10 short-answer problems (each problem is worth equal credit). Part II (60%) consists of three work-out problems (each problem is worth equal credit).

Turn in your results in the following order:

Exam questions (signed)

Ten short-answer problems (in order)

Three work-out problems (in order)

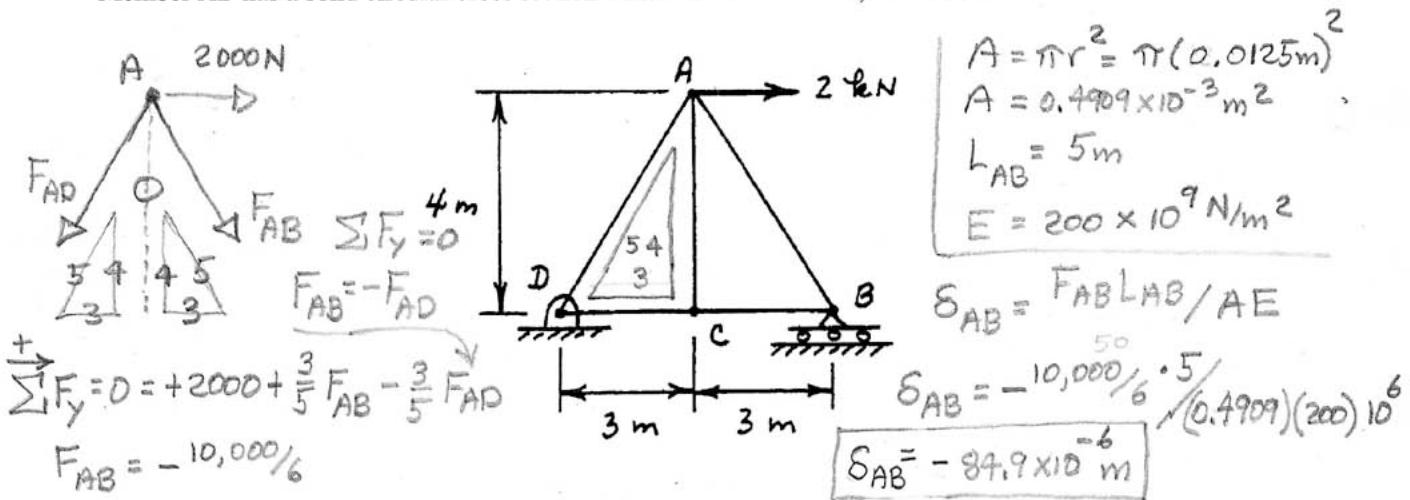
Staple the above in the upper left-hand corner.

CHECK FOR COMPLETENESS

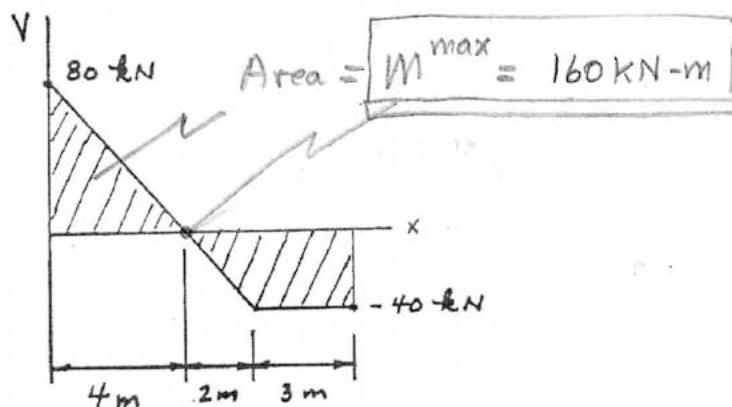
Practice Final Exam #1, pfe1.pdf

Part I

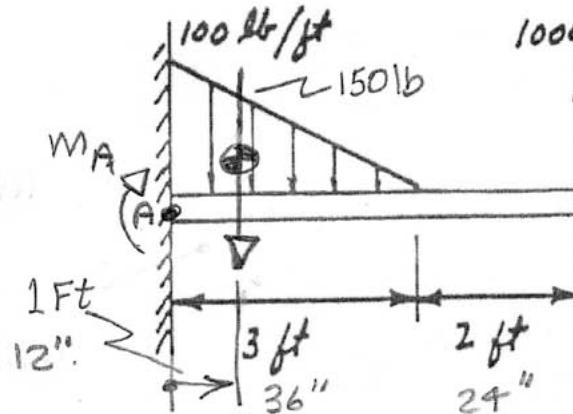
1. Determine the change in the length of member AB of the truss shown. Neglect the effects of buckling. Member AB has a solid circular cross section with a 25 mm diameter; $E = 200 \text{ GPa}$.



2. The shear diagram for a beam simply supported at the ends is shown. There are no concentrated moments acting on the beam. Determine the magnitude of the maximum bending moment.



3. For the beam loaded as shown, determine the moment at the wall.



$$\text{Sum of moments at } A = 0 =$$

$$-M_A - (12') 150 \text{ lb} + (60') 1000 \text{ lb} = 0$$

$$+ 60,000$$

$$M_A = +58,200 \text{ in-lb}$$

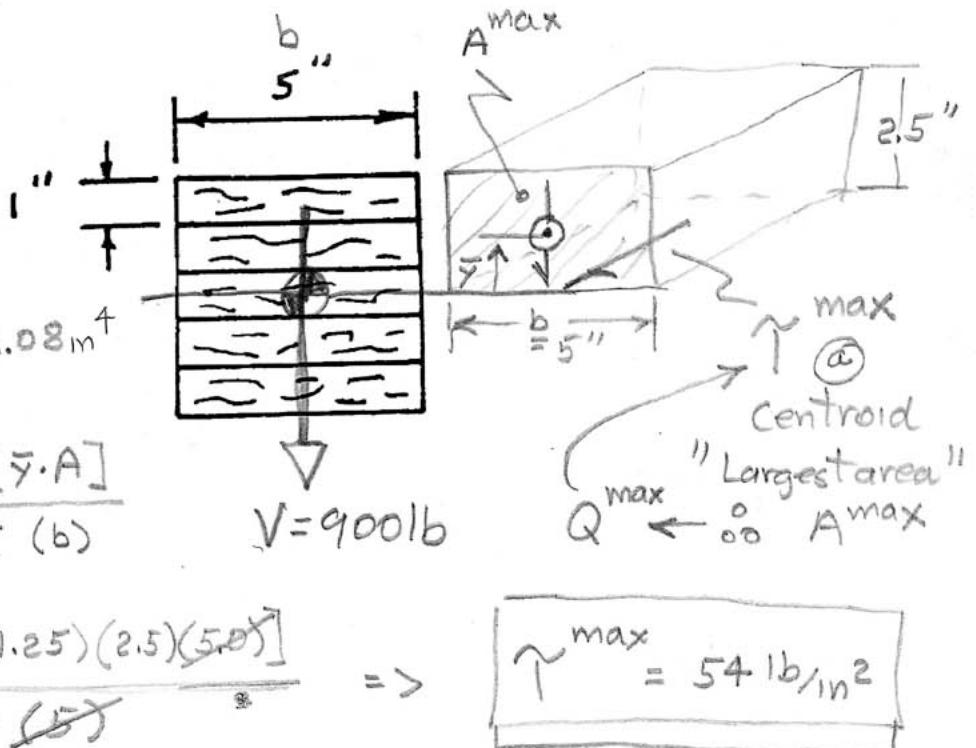
4. A beam is made by gluing five 1×5 in. boards together. For a vertical shear of 900 lb., determine the maximum shearing stress in the wood.

$$I = \frac{bh^3}{12}$$

$$= \frac{5(5)^3}{12} = 52.08 \text{ in}^4$$

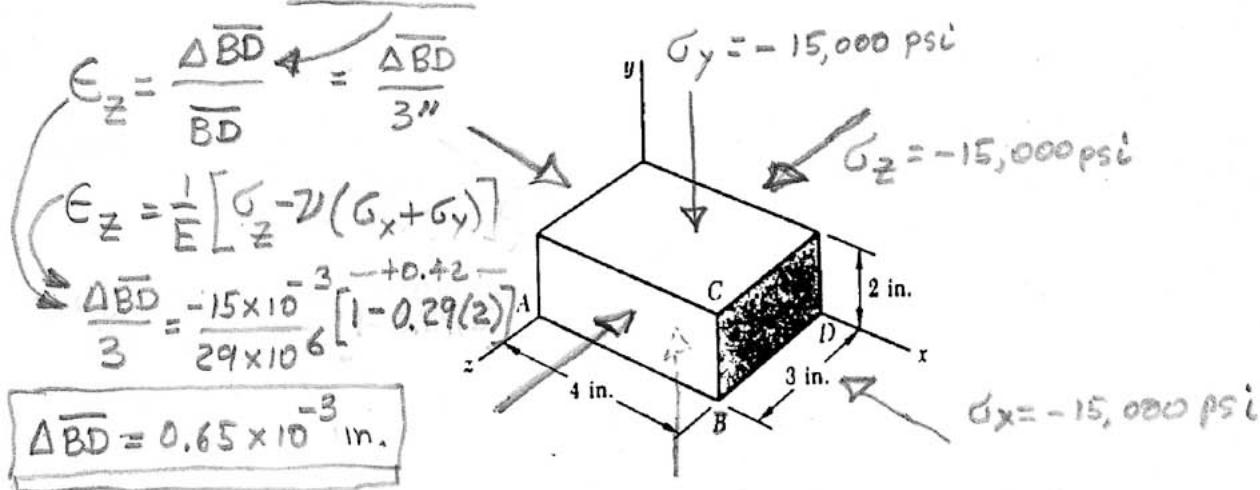
$$\tau = \frac{VQ}{It} = \frac{V[\bar{y} \cdot A]}{I(b)}$$

$$\tau^{\max} = \frac{900 \text{ lb}}{52.08 \text{ in}^4} \frac{[(1.25)(2.5)(5.0)]}{5} \Rightarrow$$

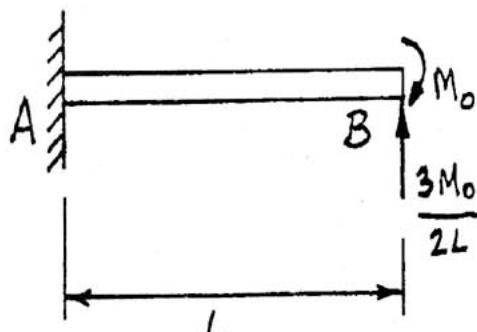


$$\tau^{\max} = 54 \text{ lb/in}^2$$

5. The steel block ($E = 29 \times 10^6$ psi, $v = 0.29$) is subjected to a uniform pressure of 15 ksi on all of its faces. Determine the change in length of the 3 in. side of the block.



6. Determine the slope at the end B of the beam loaded as shown.



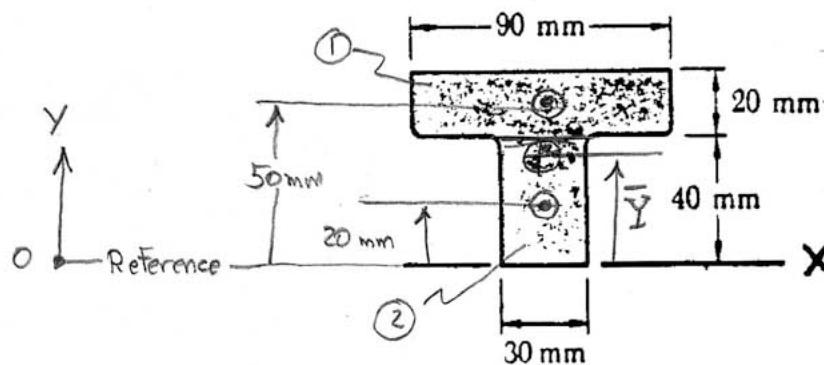
$$\text{Case 1 } \theta_B = -\frac{PL^2}{2EI} = +\frac{(3M_0/2L)L^2}{2EI}$$

$$\text{Case 3 } \theta_B = -\frac{ML}{EI} = -\frac{M_0 L}{EI}$$

Superpose
X

$$\theta_B = \frac{3}{4} \frac{M_0 L}{EI} - \frac{M_0 L}{EI} \Rightarrow \boxed{\theta_B = -\frac{M_0 L}{4EI}}$$

7. Determine the moment of inertia of the shaded area with respect of the x -axis.



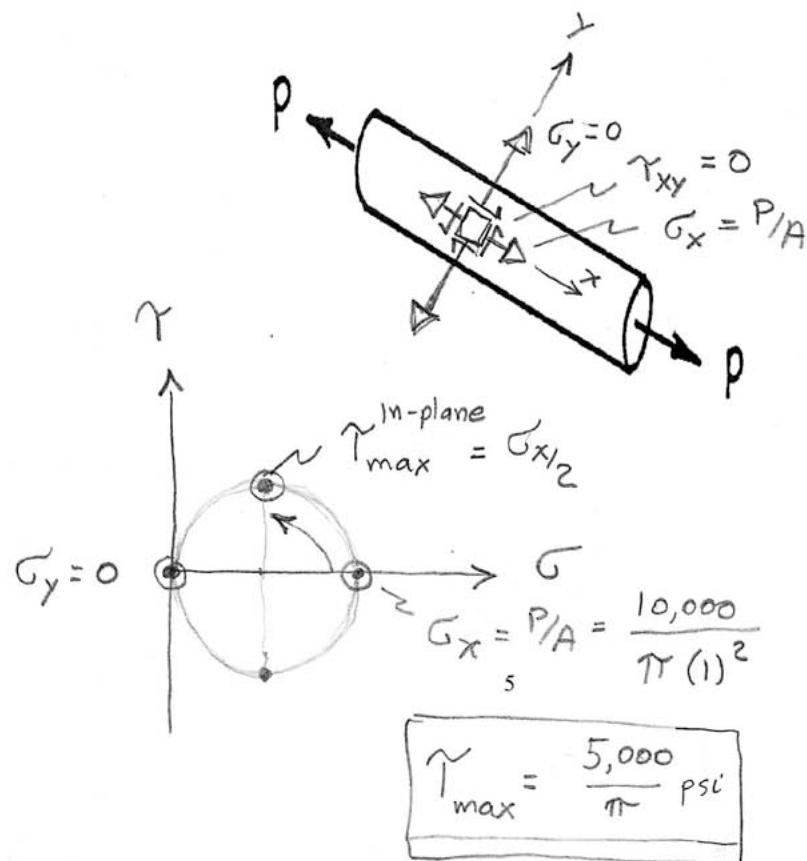
Region n	\bar{y}	A	$\bar{y}A$
(1)	50	1800	90,000
(2)	20	1200	24,000

$$\sum A = 3,000 \quad \sum \bar{y}A = 114,000$$

$$\bar{\bar{Y}} = \frac{\sum \bar{y}A}{\sum A} = \frac{114,000}{3,000}$$

$$\bar{\bar{Y}} = 38 \text{ mm}$$

8. The 2-in. diameter solid circular shaft is subjected to a centric force $P = 10,000 \text{ lb}$. Determine the maximum shearing stress.



9. The column has a 2×2 -in. cross section and is made of aluminum ($E = 10 \times 10^6$ psi, $\alpha = 12 \times 10^{-6}/^\circ\text{F}$). Determine the change in the temperature that will cause the column to buckle.

$$\frac{\pi^2 EI^4}{A E L^2} = \alpha \Delta T$$

$$\Delta T = \frac{I \pi^2 4}{A \alpha L^2}$$

$$\Delta T = \frac{4 \cdot \pi^2 \cdot 4}{4 \cdot 12 \times 10^{-6} \cdot (96)^2} = 331.776 \times 10^{-3}$$

$$\boxed{\Delta T = 119^\circ\text{F}}$$

$$I = \frac{bh^3}{12} = \frac{16}{12} = \frac{4}{3} \text{ in}^4$$

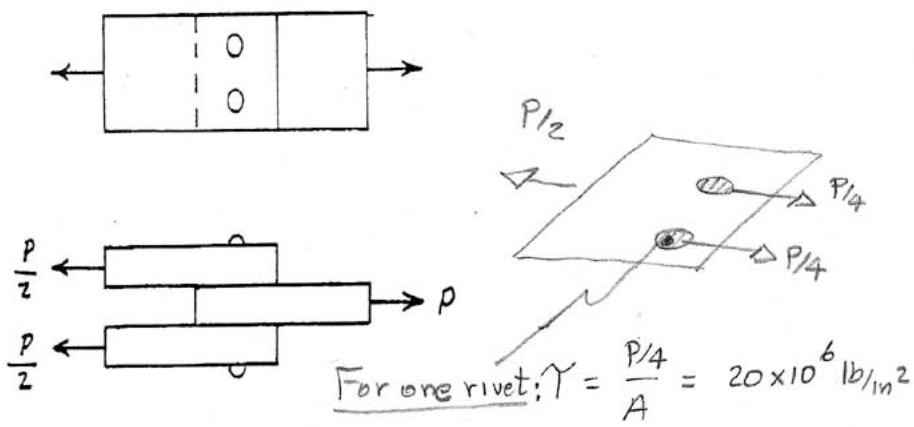
$$\delta^T = \alpha \cdot \Delta T \cdot L$$

$$P_{cr} = \frac{\pi^2 EI}{L_e^2}$$

$$L_e = L/2$$

$$\delta^P = \frac{P_{cr} L}{AE} = \alpha \Delta T + \ell$$

10. Two 0.5-in. diameter rivets are used to connect the three steel plates. If the allowable shearing stress in the rivets is 20 ksi, determine the largest load P that may be applied.



$$A = \pi (0.25)^2 = 16 \pi$$

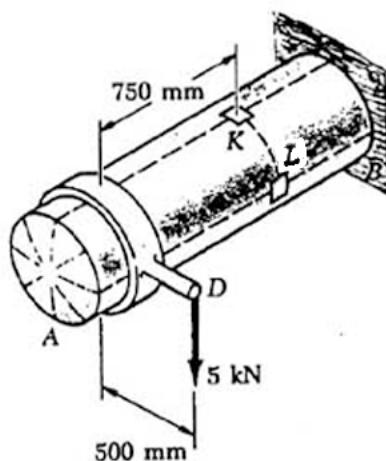
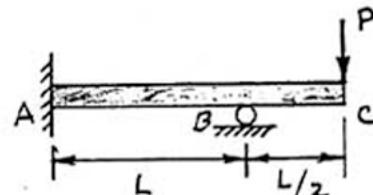
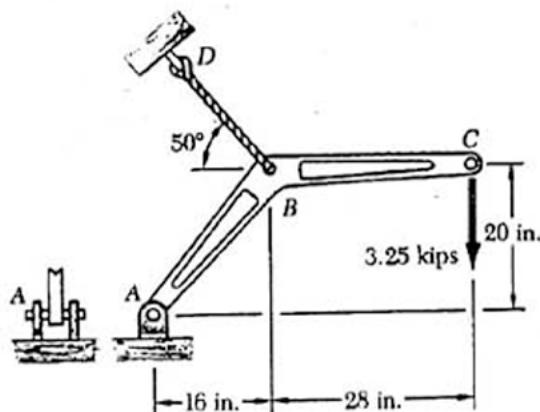
$$\frac{P}{64\pi} = 20 \times 10^6$$

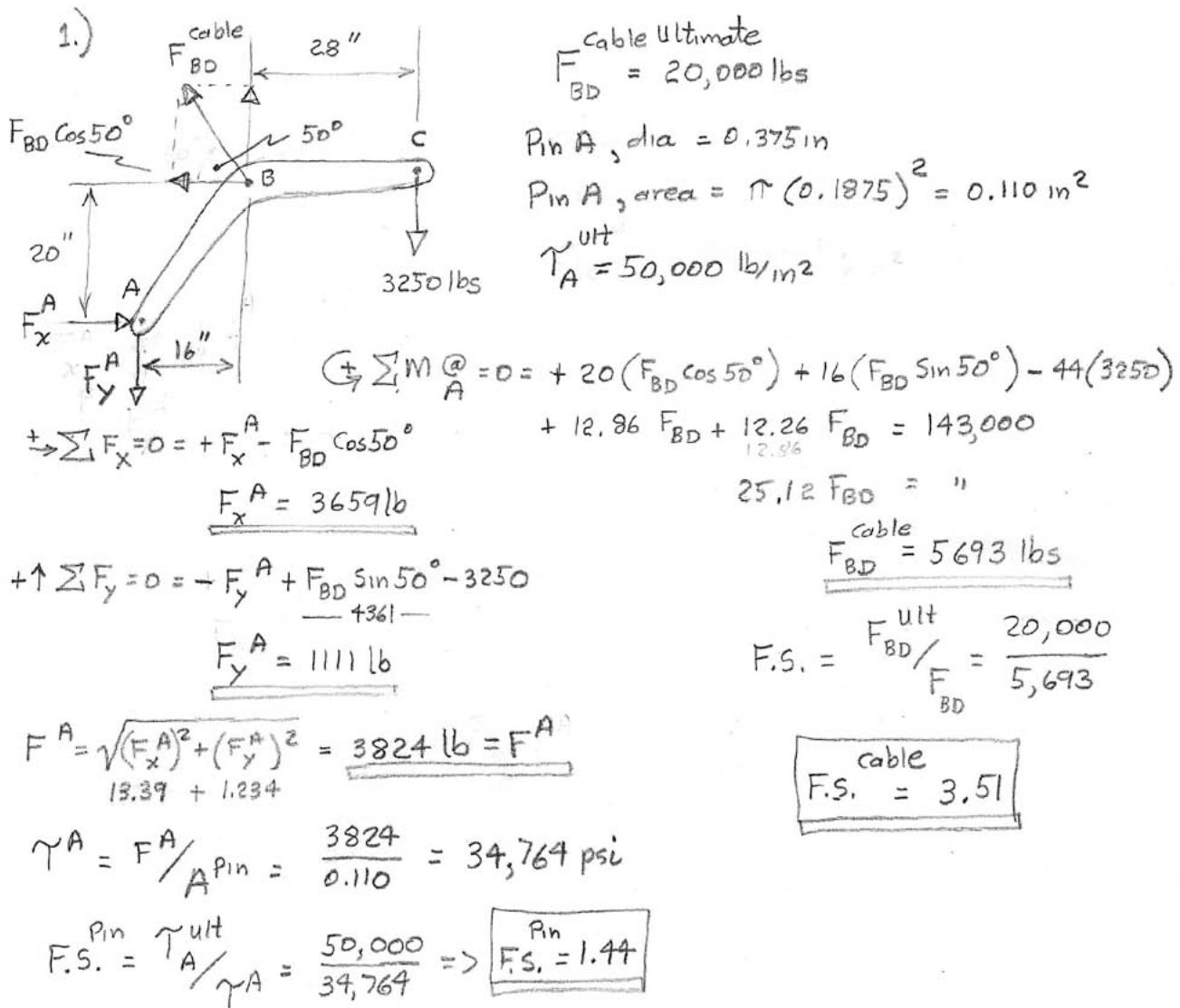
$$P = 64(\pi)(20 \times 10^6)$$

$$\boxed{P = 4.02 \times 10^9 \text{ lb}}$$

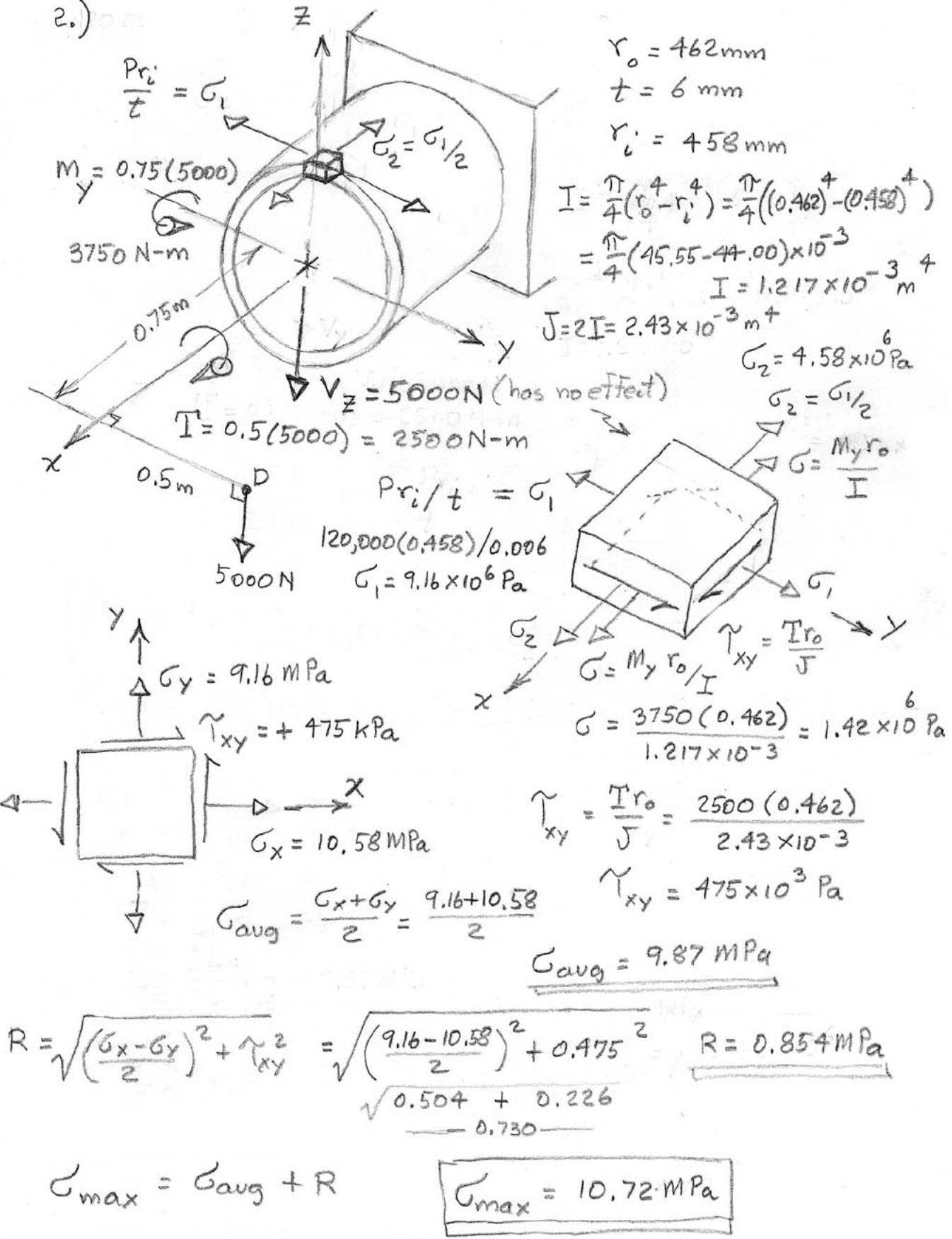
Part II

1. Cable BD has a breaking strength of 20 kips, and the pin at A has a diameter of 0.375 in. and is made of steel with an ultimate shearing stress of 50 ksi. Determine the factor of safety for the loading shown.
2. The compressed air vessel shown in the figure for Problem 2 has an outside diameter of 462 mm and a wall thickness of 6 mm. Knowing that the gage pressure inside the vessel is 120 kPa, determine the magnitude of the maximum normal stress at point K.
3. Determine the reactions at A and B for the beam loaded and supported as shown in the figure for Problem 3.

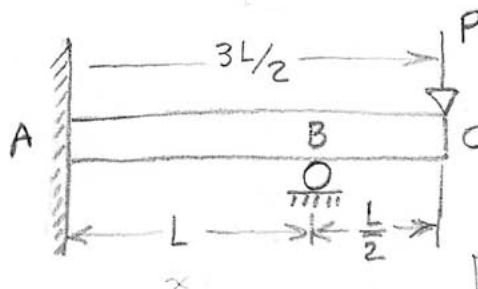




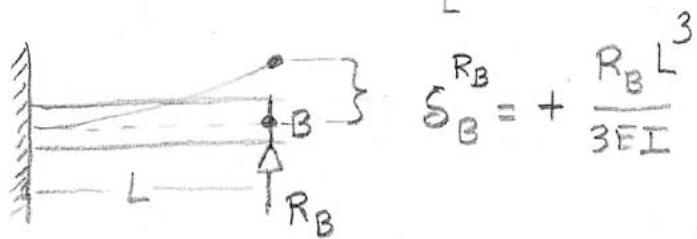
2.)



3.)



$$\left[\text{Case 1 : } S = \frac{PL^3}{3E} \right]$$



$$+ \left[\text{Case 1 : } Y_{(x)} = \frac{P}{6EI} (x^3 - 3Lx^2) \right]$$

$$+ \left. \begin{array}{l} \\ Y_{(x=L)}^B = + \frac{P}{6EI} \left(L^3 - 3 \left(\frac{3L}{2} \right) L^2 \right) \end{array} \right\}$$

$$S_B = 0 = S_B^{R_B} + Y_{(x=L)}^B = \frac{R_B L^3}{3EI} + \frac{P}{6EI} \left(L^3 - 3 \left(\frac{3L}{2} \right) L^2 \right) = 0$$

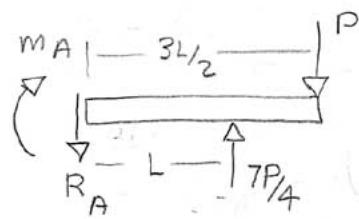
$$0 = \frac{R_B L^3}{3} + \frac{P}{6} \left(L^3 - \frac{9}{2} L^3 \right); \quad R_B = -\frac{3}{6} P \left(1 - \frac{9}{2} \right)$$

$$R_B = -\frac{P}{2} \left(\frac{2}{2} - \frac{9}{2} \right)$$

$$R_B = +\frac{7}{4} P$$

Overall FBD

$$R_A = \frac{3}{4} P \downarrow$$



$$\begin{aligned} \text{At } \sum M_A &= 0 = -M_A \\ &+ \frac{7PL}{4} - \frac{6PL}{8} \end{aligned}$$

$$\boxed{M_A = PL/4}$$